

$$\text{Area bounded} = \int_{-1}^1 \left(\frac{1}{1+y^2} - \frac{y^2}{2} \right) dy$$

$$= \left(\tan^{-1} y - \frac{y^3}{6} \right) \Big|_{-1}^1$$

$$= \frac{\pi}{2} - \frac{1}{3}$$

10. Let $A = \begin{bmatrix} \frac{1}{\sqrt{2}} & -2 \\ 0 & 1 \end{bmatrix}$ and $P = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$, $\theta > 0$. If $B = PAP^T$, $C = P^T B^{10} P$ and the sum of the diagonal elements of C is $\frac{m}{n}$, where $\text{gcd}(m, n) = 1$, then $m + n$ is :

(1) 65 (2) 127
(3) 258 (4) 2049

Ans. (1)

Sol. $P = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$

$$\therefore P^T P = I$$

$$B = PAP^T$$

Pre multiply by P^T (Given)

$$P^T B = P^T P A P^T = A P^T$$

Now post multiply by P

$$P^T B P = A P^T P = A$$

$$\text{So } A^2 = \underbrace{P^T B P}_{I} \underbrace{P^T}_{P} B P$$

$$A^2 = P^T B^2 P$$

$$\text{Similarly } A^{10} = P^T B^{10} P = C$$

$$A = \begin{bmatrix} \frac{1}{\sqrt{2}} & -2 \\ 0 & 1 \end{bmatrix} \text{ (Given)}$$

$$\Rightarrow A^2 = \begin{bmatrix} \frac{1}{2} & -\sqrt{2} - 2 \\ 0 & 1 \end{bmatrix}$$

Similarly check A^3 and so on since $C = A^{10}$

$$\Rightarrow \text{Sum of diagonal elements of } C \text{ is } \left(\frac{1}{\sqrt{2}} \right)^{10} + 1$$

$$= \frac{1}{32} + 1 = \frac{33}{32} = \frac{m}{n}$$

$\text{g cd}(m, n) = 1$ (Given)

$$\Rightarrow m + n = 65$$

11. If $f(x) = \int \frac{1}{x^{1/4}(1+x^{1/4})} dx$, $f(0) = -6$, then $f(1)$ is equal to :

(1) $\log_e 2 + 2$ (2) $4(\log_e 2 - 2)$
(3) $2 - \log_e 2$ (4) $4(\log_e 2 + 2)$

Ans. (2)

Sol. let $x = t^4$

$$dx = 4t^3 dt$$

$$\text{then } \int \frac{1}{x^{\frac{1}{4}} \left(1 + x^{\frac{1}{4}} \right)} dx \Rightarrow \int \frac{4t^3 dt}{t(1+t)}$$

$$\Rightarrow \int \frac{4t}{1+t} dt \Rightarrow 4 \int \frac{(t^2 - 1) + 1}{1+t} dt$$

$$\Rightarrow 4 \int (t-1) + \frac{1}{t+1} dt$$

$$\Rightarrow 4 \left\{ \frac{(t-1)^2}{2} + \ell \ln(t+1) \right\} + C$$

$$\text{hence } f(x) = 2 \left(x^{\frac{1}{4}} - 1 \right)^2 + 4 \ell \ln \left(1 + x^{\frac{1}{4}} \right) + C$$

$$f(0) = -6 \Rightarrow 2 + 4 \ell \ln 1 + 6 = -6 \rightarrow C = -8$$

$$\text{now } f(1) = 4 \ell \ln 2 - 8$$

$$= 4(\ell \ln 2 - 2)$$

12. Let $f : R \rightarrow R$ be a twice differentiable function such that $f(2) = 1$. If $F(x) = xf(x)$ for all $x \in R$,

$$\int_0^2 x F'(x) dx = 6 \text{ and } \int_0^2 x^2 F''(x) dx = 40, \text{ then}$$

$$F'(2) + \int_0^2 F(x) dx \text{ is equal to :}$$

(1) 11 (2) 15
(3) 9 (4) 13

Ans. (1)

19. If A and B are the points of intersection of the circle $x^2 + y^2 - 8x = 0$ and the hyperbola $\frac{x^2}{9} - \frac{y^2}{4} = 1$ and a point P moves on the line

$2x - 3y + 4 = 0$, then the centroid of ΔPAB lies on the line :

- (1) $4x - 9y = 12$
- (2) $x + 9y = 36$
- (3) $9x - 9y = 32$
- (4) $6x - 9y = 20$

Ans. (4)

Sol. $x^2 + y^2 - 8x = 0, \frac{x^2}{9} - \frac{y^2}{4} = 1$ (1)

$4x^2 - 9y^2 = 36$... (2)

Solve (1) & (2)

$$4x^2 - 9(8x - x^2) = 36$$

$$13x^2 - 72x - 36 = 0$$

$$(13x + 6)(x - 6) = 0$$

$$x = \frac{-6}{13}, x = 6$$

$$x = \frac{-6}{13} \text{ (rejected)}$$

$y \rightarrow$ Imaginary

$$n = 6, \frac{36}{9} - \frac{y^2}{4} = 1$$

$$y^2 = 12, y = \pm\sqrt{12}$$

$$A(6, \sqrt{12}), B(6, -\sqrt{12})$$

$$P\left(\alpha, \frac{2\alpha+4}{3}\right) P \text{ lies on}$$

$$\text{centroid (h,k)} \quad 2x - 3y + y = 0$$

$$h = \frac{12 + \alpha}{3}, \alpha = 3h - 12$$

$$k = \frac{\frac{2\alpha+4}{3}}{3} \Rightarrow 2\alpha + 4 = 9k$$

$$\alpha = \frac{9k - 4}{2}$$

$$6h - 2y = 9k - 4$$

$$6x - 9y = 20$$

20. Let $f : \mathbf{R} - \{0\} \rightarrow (-\infty, 1)$ be a polynomial of degree 2, satisfying $f(x)f\left(\frac{1}{x}\right) = f(x) + f\left(\frac{1}{x}\right)$. If $f(K) = -2K$, then the sum of squares of all possible values of K is :

- (1) 1
- (2) 6
- (3) 7
- (4) 9

Ans. (2)

Sol. as $f(x)$ is a polynomial of degree two let it be $f(x) = ax^2 + bx + c$ ($a \neq 0$)

on satisfying given conditions we get

$$C = 1 \text{ & } a = \pm 1$$

$$\text{hence } f(x) = 1 \pm x^2$$

also range $\in (-\infty, 1]$ hence

$$f(x) = 1 - x^2$$

$$\text{now } f(k) = -2k$$

$$1 - k^2 = -2k \rightarrow k^2 - 2k - 1 = 0$$

let roots of this equation be α & β

$$\text{then } \alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta \\ = 4 - 2(-1) = 6$$

SECTION-B

21. The number of natural numbers, between 212 and 999, such that the sum of their digits is 15, is _____.

Ans. (64)

Sol.

x	y	z
---	---	---

$$\text{Let } x = 2 \Rightarrow y + z = 13$$

$$(4,9), (5,8), (6,7), (7,6), (8,5), (9,4), \rightarrow 6$$

$$\text{Let } x = 3 \rightarrow y + z = 12$$

$$(3,9), (4,8), \dots, (9,3) \rightarrow 7$$

$$\text{Let } x = 4 \rightarrow y + z = 11$$

$$(2,9), (3,8), \dots, (9,1) \rightarrow 9$$

$$\text{Let } x = 5 \rightarrow y + z = 10$$

$$(1,9), (2,8), \dots, (9,1) \rightarrow 10$$

$$\text{Let } x = 6 \rightarrow y + z = 9$$

$$(0,9), (1,8), \dots, (9,0) \rightarrow 9$$

$$\text{Let } x = 7 \rightarrow y + z = 8$$

$$(0,9), (1,7), \dots, (8,0) \rightarrow 9$$

$$\text{Let } x = 8 \rightarrow y + z = 7$$

$$(0,7), (1,6), \dots, (7,0) \rightarrow 8$$

$$\text{Let } x = 9 \rightarrow y + z = 6$$

$$(0,6), (1,5), \dots, (6,0) \rightarrow 7$$

$$\text{Total} = 6 = 7 + 8 + 9 + 10 + 9 + 8 + 7 = 64$$

22. Let $f(x) = \lim_{n \rightarrow \infty} \sum_{r=0}^n \left(\frac{\tan(x/2^{r+1}) + \tan^3(x/2^{r+1})}{1 - \tan^2(x/2^{r+1})} \right)$.

Then $\lim_{x \rightarrow 0} \frac{e^x - e^{f(x)}}{(x - f(x))}$ is equal to ____.

Ans. (1)

Sol. $f(x) = \lim_{n \rightarrow \infty} \sum_{r=0}^n \left(\tan \frac{x}{2^r} - \tan \frac{x}{2^{r+1}} \right) = \tan x$

$$\lim_{x \rightarrow 0} \left(\frac{e^x - e^{\tan x}}{x - \tan x} \right) = \lim_{x \rightarrow 0} e^{\tan x} \frac{(e^{x - \tan x} - 1)}{(x - \tan x)} = 1$$

23. The interior angles of a polygon with n sides, are in an A.P. with common difference 6° . If the largest interior angle of the polygon is 219° , then n is equal to ____.

Ans. (20)

Sol. $\frac{n}{2}(2a + (n-1)6) = (n-2).180^\circ$

$$an + 3n^2 - 3n = (n-2).180^\circ \quad \dots(1)$$

Now according to question

$$a + (n-1)6^\circ = 219^\circ$$

$$\Rightarrow a = 225^\circ - 6n^\circ \quad \dots(2)$$

Putting value of a from equation (2) in (1)

We get

$$(225n - 6n^2) + 3n^2 - 3n = 180n - 360$$

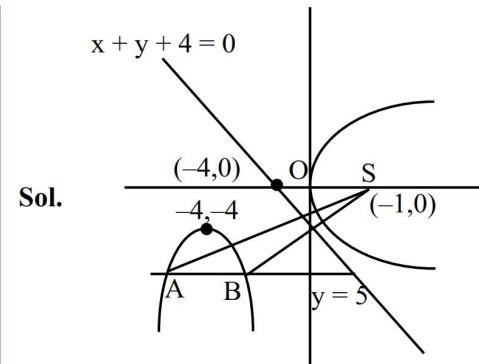
$$\Rightarrow 2n^2 - 42n - 360 = 0$$

$$\Rightarrow n^2 - 21n - 180 = 0$$

$$n = 20, -6(\text{rejected})$$

24. Let A and B be the two points of intersection of the line $y + 5 = 0$ and the mirror image of the parabola $y^2 = 4x$ with respect to the line $x + y + 4 = 0$. If d denotes the distance between A and B , and a denotes the area of ΔSAB , where S is the focus of the parabola $y^2 = 4x$, then the value of $(a + d)$ is ____.

Ans. (14)



$$\text{Area} = \frac{1}{2} \times 4 \times 5 = 10 = a$$

$$6 = 4$$

$$\text{So } a + d = 14$$

25. If $y = y(x)$ is the solution of the differential equation,

$$\sqrt{4-x^2} \frac{dy}{dx} = \left(\left(\sin^{-1} \left(\frac{x}{2} \right) \right)^2 - y \right) \sin^{-1} \left(\frac{x}{2} \right),$$

$$-2 \leq x \leq 2, y(2) = \left(\frac{\pi^2 - 8}{4} \right), \text{ then } y^2(0) \text{ is equal to } \dots$$

Ans. (4)

Sol. $\frac{dy}{dx} + \frac{\left(\sin^{-1} \frac{x}{2} \right)}{\sqrt{4-x^2}} y = \frac{\left(\sin^{-3} \frac{x}{2} \right)^3}{\sqrt{4-x^2}}$

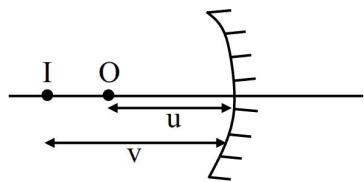
$$y e^{\int \frac{\left(\sin^{-1} \frac{x}{2} \right)}{\sqrt{4-x^2}} dx} = \int \frac{\left(\sin^{-3} \frac{x}{2} \right)^3}{4-x^2} e^{\int \frac{\left(\sin^{-1} \frac{x}{2} \right)}{\sqrt{4-x^2}} dx} dx$$

$$y = \left(\sin^{-1} \frac{x}{2} \right)^2 - 2 + c.e^{-\left(\sin^{-1} \frac{x}{2} \right)^2}$$

$$y(2) = \frac{\pi^2}{4} - 2 \Rightarrow c = 0$$

$$y(0) = -2$$

Sol.



$$m = -3 = -\frac{v}{u} \text{ and } v - u = 20 \text{ cm}$$

$$f = \frac{vu}{v+u} = \frac{(-30)(-10)}{-30-10}$$

$$\therefore R = +15$$

39. A body of mass 4 kg is placed on a plane at a point P having coordinate $(3, 4)$ m. Under the action of force $\vec{F} = (2\hat{i} + 3\hat{j})$ N, it moves to a new point Q having coordinates $(6, 10)$ m in 4 sec. The average power and instantaneous power at the end of 4 sec are in the ratio of :

Ans. (2)

$$\text{Sol. } \langle \mathbf{p} \rangle = \frac{(2\hat{\mathbf{i}} + 3\hat{\mathbf{j}}) \cdot (3\hat{\mathbf{i}} + 6\hat{\mathbf{j}})}{4} = 6$$

$$\vec{a} = \left(\frac{\vec{F}}{m} = \frac{1}{2} \hat{i} + \frac{3}{4} \hat{j} \right)$$

$$\vec{v} \text{ at } t = 4 \text{ sec} = \left(\frac{1}{2} \hat{i} + \frac{3}{4} \hat{j} \right) \times 4 = (2\hat{i} + 3\hat{j})$$

$$P_{ins} = (2\hat{i} + 3)(2\hat{i} + 3\hat{j}) = 13$$

$$\frac{< P >}{P_{ins}} = \frac{6}{13}$$

Note : Given data is not matching.

$$S = ut + \frac{1}{2}at^2$$

$$S = 0 + \frac{1}{2} \frac{(2\hat{i} + 3\hat{j})}{4} (4)^2 = 4\hat{i} + 6\hat{j}$$

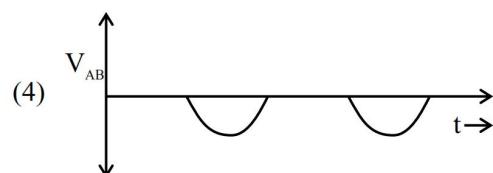
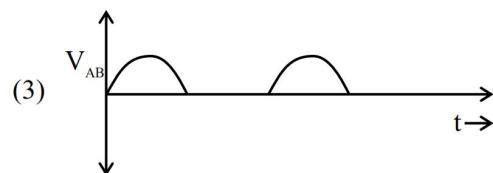
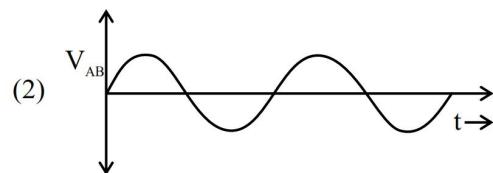
If $\vec{r}_i = 3\hat{i} + 4\hat{j}$ then $\vec{r}_f = 7\hat{i} + 10\hat{j}$

But Final position given in the question is (6, 10).

40.

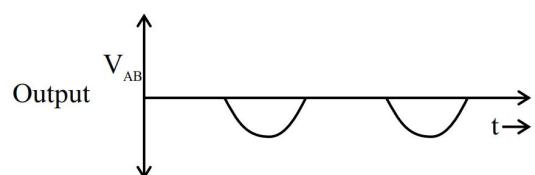
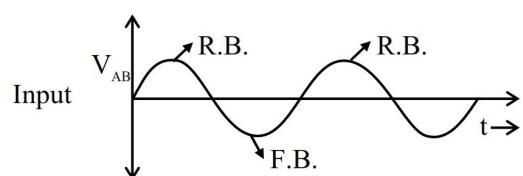
In the circuit shown here, assuming threshold voltage of diode is negligibly small, then voltage V_{AB} is correctly represented by :

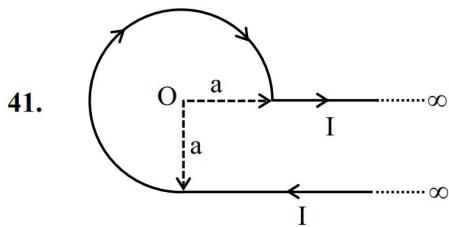
(1) V_{AB} would be zero at all times



Ans. (4)

Sol. $V = V_0 \sin \omega t$



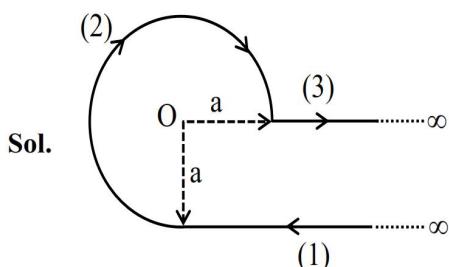


41.

An infinite wire has a circular bend of radius a , and carrying a current I as shown in figure. The magnitude of magnetic field at the origin O of the arc is given by :

(1) $\frac{\mu_0}{4\pi a} I \left[\frac{\pi}{2} + 1 \right]$ (2) $\frac{\mu_0}{4\pi a} I \left[\frac{3\pi}{2} + 1 \right]$
 (3) $\frac{\mu_0}{2\pi a} I \left[\frac{\pi}{2} + 2 \right]$ (4) $\frac{\mu_0}{4\pi a} I \left[\frac{3\pi}{2} + 2 \right]$

Ans. (2)



Sol.

$$B_1 = \frac{\mu_0 i}{4\pi a} \otimes$$

$$B_2 = \frac{\mu_0 i}{4\pi a} \left(\frac{3\pi}{2} \right) \otimes$$

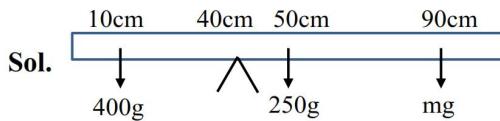
$$B_3 = 0$$

$$B = \frac{\mu_0 i}{4\pi a} \left(1 \frac{3\pi}{2} \right) \otimes$$

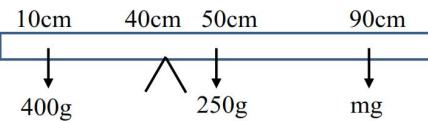
42. A uniform rod of mass 250 g having length 100 cm is balanced on a sharp edge at 40 cm mark. A mass of 400 g is suspended at 10 cm mark. To maintain the balance of the rod, the mass to be suspended at 90 cm mark, is

(1) 300 g (2) 190 g
 (3) 200 g (4) 290 g

Ans. (2)



Sol.



$$\tau_{\text{Net}} = 0 \Rightarrow (400g \times 30) = (250g \times 10) (mg \times 50)$$

$$m = \frac{12000 - 2500}{50} = \frac{9500}{50}$$

$$M = 190 \text{ g}$$

43. a 400 g solid cube having an edge of length 10 cm floats in water. How much volume of the cube is outside the water ?

(Given : density of water = 1000 kg m^{-3})

(1) 1400 cm^3 (2) 4000 cm^3
 (3) 400 cm^3 (4) 600 cm^3

Ans. (4)

$$Mg = F_B \Rightarrow (400 \times 10^{-3}) = 10^3 \times V_d$$

$$V_d = 400 \times 10^{-6} \text{ m}^3$$

$$(\text{Vol.})_{\text{outside}} = (10 \times 10^{-2})^3 - 400 \times 10^{-6} = 600 \times 10^{-6} \text{ m}^3 = 600 \text{ cm}^3$$

44. The magnetic field of an E.M. wave is given by

$$\vec{B} = \left(\frac{\sqrt{3}}{2} \hat{i} + \frac{1}{2} \hat{j} \right) 30 \sin \left[\omega \left(t - \frac{z}{c} \right) \right] \text{ (S.I. Units)}$$

The corresponding electric field in S.I. units is :

$$(1) \vec{E} = \left(\frac{1}{2} \hat{i} - \frac{\sqrt{3}}{2} \hat{j} \right) 30c \sin \left[\omega \left(t - \frac{z}{c} \right) \right]$$

$$(2) \vec{E} = \left(\frac{3}{4} \hat{i} + \frac{1}{4} \hat{j} \right) 30c \cos \left[\omega \left(t - \frac{z}{c} \right) \right]$$

$$(3) \vec{E} = \left(\frac{1}{2} \hat{i} + \frac{\sqrt{3}}{2} \hat{j} \right) 30c \sin \left[\omega \left(t + \frac{z}{c} \right) \right]$$

$$(4) \vec{E} = \left(\frac{\sqrt{3}}{2} \hat{i} - \frac{1}{2} \hat{j} \right) 30c \sin \left[\omega \left(t + \frac{z}{c} \right) \right]$$

Ans. (1)

$$\vec{B} = \left(\frac{\sqrt{3}}{2} \hat{i} + \frac{1}{2} \hat{j} \right) 30 \sin \left[\omega \left(t - \frac{z}{c} \right) \right]$$

$$\vec{E} = \vec{B} \times \vec{c} \text{ and } E = B_0 c$$

$$\text{Here } \vec{E} = \left(\frac{\sqrt{3}}{2} (-\hat{j}) + \frac{1}{2} \hat{i} \right) 30c \sin \left[\omega \left(t - \frac{z}{c} \right) \right]$$

$$E_0 = 30c$$

$$\vec{E} = \left(\frac{1}{2} \hat{i} - \frac{\sqrt{3}}{2} \hat{j} \right) 30c \sin \left[\omega \left(t - \frac{z}{c} \right) \right]$$

45. A balloon and its content having mass M is moving up with an acceleration ' a '. The mass that must be released from the content so that the balloon starts moving up with an acceleration ' $3a$ ' will be : (Take ' g ' as acceleration due to gravity)

(1) $\frac{3Ma}{2a-g}$

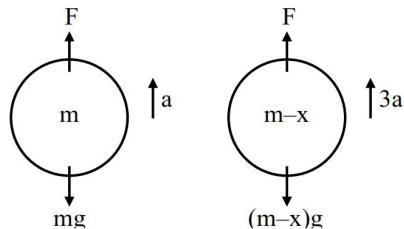
(2) $\frac{3Ma}{2a+g}$

(3) $\frac{2Ma}{3a+g}$

(4) $\frac{2Ma}{3a-g}$

Ans. (3)

Sol.



$$F - mg = ma$$

$$F = ma + mg$$

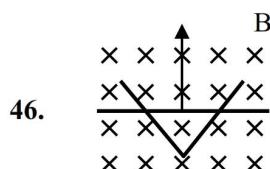
$$F - (m-x)g = (m-x) 3a$$

Put F

$$Ma + mg - mg + xg = 3ma - 3xa$$

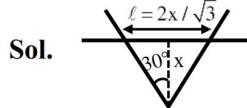
$$x = \frac{2ma}{g + 3a}$$

SECTION-B



46. A conducting bar moves on two conducting rails as shown in the figure. A constant magnetic field B exists into the page. The bar starts to move from the vertex at time $t = 0$ with a constant velocity. If the induced EMF is $E \propto t^n$, then value of n is ____.

Ans. (1)



$$E = \ell v B$$

$$E = \frac{2x}{\sqrt{3}} \times v B \text{ and } x = vt$$

$$E = \frac{2}{\sqrt{3}} v^2 B t$$

$$E \propto t^1$$

47. An electric dipole of dipole moment 6×10^{-6} Cm is placed in uniform electric field of magnitude 10^6 V/m. Initially, the dipole moment is parallel to electric field. The work that needs to be done on the dipole to make its dipole moment opposite to the field, will be ____ J.

Ans. (12)

Sol. $p = 6 \times 10^{-6}$ Cm

$$E = 10^6 \text{ V/m}$$

$$W = \Delta U = -pE(\cos\theta_f - \cos\theta_i)$$

$$W = 2pE = 12 \text{ J}$$

48. The volume contraction of a solid copper cube of edge length 10 cm, when subjected to a hydraulic pressure of 7×10^6 Pa, would be ____ mm³.
(Given bulk modulus of copper = 1.4×10^{11} Nm⁻²)

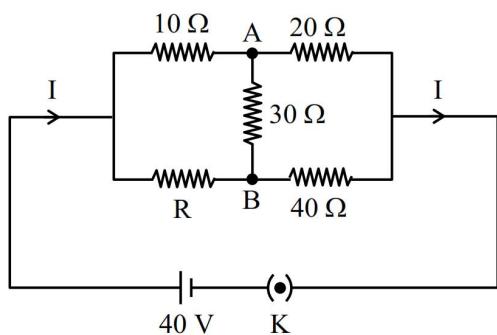
Ans. (50)

Sol. $B = \frac{\Delta P}{\frac{\Delta V}{V}}$

$$\Delta V = \frac{7 \times 10^6}{1.4 \times 10^{11}} \times (10 \times 10^{-2})^3$$

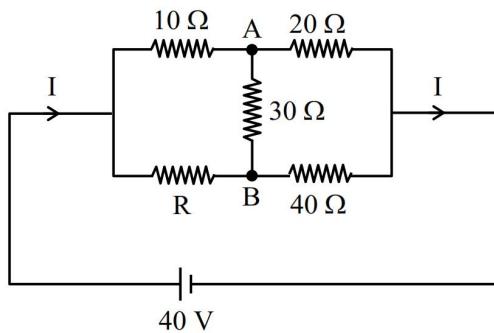
$$\Delta V = 50 \text{ mm}^3$$

49. The value of current I in the electrical circuit as given below, when potential at A is equal to the potential at B, will be _____ A.



Ans. (2)

Sol.



$V_A = V_B \Rightarrow$ the bridge is balanced

$$\Rightarrow \frac{10}{R} = \frac{20}{40}$$

$$R = 20\Omega$$

$$I = \frac{40}{20} = 2A$$

50. A thin transparent film with refractive index 1.4, is held on circular ring of radius 1.8 cm. The fluid in the film evaporates such that transmission through the film at wavelength 560 nm goes to a minimum every 12 seconds. Assuming that the film is flat on its two sides, the rate of evaporation is _____ $\pi \times 10^{-13} \text{ m}^3/\text{s}$.

Ans. (54)

Sol. Maxima condition

$$2\mu t = n\lambda \Rightarrow t = \frac{n\lambda}{2\mu} \Rightarrow t = \frac{\lambda}{2\mu}, \frac{2\lambda}{2\mu}, \dots$$

$$\text{Minima condition } 2\mu t = (2n-1)\lambda/2$$

$$\Rightarrow t = \frac{(2n-1)\lambda}{4\mu} \Rightarrow t = \frac{\lambda}{4\mu}, \frac{3\lambda}{4\mu}, \dots$$

$$\Delta t = \frac{2\lambda}{4\mu}$$

$$\text{Rate of evaporation} = \frac{A(\Delta t)}{\text{time}} = 54 \times 10^{-13} \text{ m}^3/\text{s}$$

CHEMISTRY

SECTION-A

51. consider the elementary reaction



If the volume of reaction mixture is suddenly reduced to $\frac{1}{3}$ of its initial volume, the reaction rate will become 'x' times of the original reaction rate. The value of x is :

(1) $\frac{1}{9}$

(2) 9

(3) $\frac{1}{3}$

(4) 3

Ans. (2)

Sol. $R_1 = K[A]^1 [B]^1$

$$R_1 = K \left[\frac{n_A}{V} \right]^1 \left[\frac{n_B}{V} \right]^1$$

$$R_2 = K \left[\frac{3n_A}{V} \right]^1 \left[\frac{3n_B}{V} \right]^1$$

$$R_2 = 9R_1$$

52. The amphoteric oxide among V_2O_3 , V_2O_4 and V_2O_5 upon reaction with alkali leads to formation of an oxide anion. The oxidation state of V in the oxide anion is :

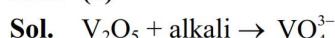
(1) +3

(2) +7

(3) +5

(4) +4

Ans. (3)



In VO_4^{3-} ion, vanadium is in +5 oxidation state

53. Match List-I with List-II

List-I
(Saccharides)

List-II
(Glycosidic-linkages found)

(A) Sucrose

(I) $\alpha 1 - 4$

(B) Maltose

(II) $\alpha 1 - 4$ and $\alpha 1 - 6$

(C) Lactose

(III) $\alpha 1 - \beta 2$

(D) Amylopectin

(IV) $\beta 1 - 4$

Choose the correct answer from the options given below :

(1) (A)-(III), (B)-(I), (C)-(IV), (D)-(II)

(2) (A)-(IV), (B)-(II), (C)-(I), (D)-(III)

(3) (A)-(II), (B)-(IV), (C)-(III), (D)-(I)

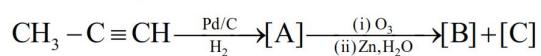
(4) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)

Ans. (1)

Sol. (A) Sucrose $\rightarrow \alpha_1 - \beta_2$ Glycosidic linkage
 (B) Maltose $\rightarrow \alpha 1 - 4$ Glycosidic linkage
 (C) Lactose $\rightarrow \beta 1 - 4$ Glycosidic linkage
 (D) Amylopectin $\rightarrow \alpha 1 - 4$ and $\alpha 1 - 6$ Glycosidic linkage

A-III, B-I, C-IV, D-II

54. Identify product [A], [B] and [C] in the following reaction sequence :



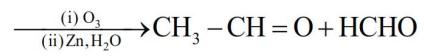
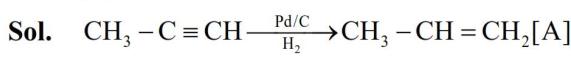
(1) [A] : $CH_3 - CH = CH_2$, [B] : CH_3CHO ,
 [C] : $HCHO$

(2) [A] : $CH_2 = CH_2$, [B] : $\begin{matrix} O \\ || \\ H_3C - C - CH_3 \end{matrix}$,
 [C] : $HCHO$

(3) [A] : $CH_3 - CH = CH_2$, [B] : CH_3CHO ,
 [C] : CH_3CH_2OH

(4) [A] : $CH_3CH_2CH_3$, [B] : CH_3CHO , [C] : $HCHO$

Ans. (1)



[B] [C]

55. Arrange the following in increasing order of solubility product :

$Ca(OH)_2, AgBr, PbS, HgS$

(1) $PbS < HgS < Ca(OH)_2 < AgBr$

(2) $HgS < PbS < AgBr < Ca(OH)_2$

(3) $Ca(OH)_2 < AgBr < HgS < PbS$

(4) $HgS < AgBr < PbS < Ca(OH)_2$

Ans. (2)

Sol. Based on the K_{sp} values and salt analysis cation identification, we can say that order of K_{sp} value is:

$HgS < PbS < AgBr < Ca(OH)_2$

K_{sp} values

$HgS \rightarrow 4 \times 10^{-53}$

$PbS \rightarrow 8 \times 10^{-28}$

$AgBr \rightarrow 5 \times 10^{-13}$

$Ca(OH)_2 \rightarrow 5.5 \times 10^{-6}$

61. Match List-I with List-II.

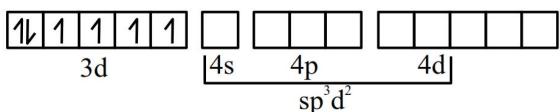
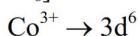
List-I (Complex)	List-II (Hybridisation of central metal ion)
(A) $[\text{CoF}_6]^{3-}$	(I) d^2sp^3
(B) $[\text{NiCl}_4]^{2-}$	(II) sp^3
(C) $[\text{Co}(\text{NH}_3)_6]^{3+}$	(III) sp^3d^2
(D) $[\text{Ni}(\text{CN})_4]^{2-}$	(IV) dsp^2

Choose the **correct** answer from the options given below :

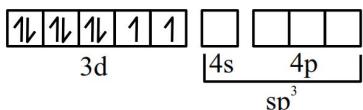
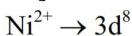
- (1) (A)-(I), (B)-(IV), (C)-(III), (D)-(II)
- (2) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
- (3) (A)-(I), (B)-(II), (C)-(III), (D)-(IV)
- (4) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

Ans. (2)

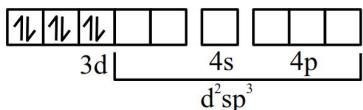
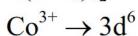
Sol. (A) $[\text{CoF}_6]^{3-}$



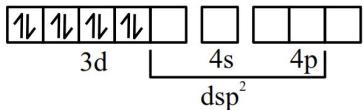
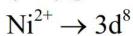
(B) $[\text{NiCl}_4]^{2-}$



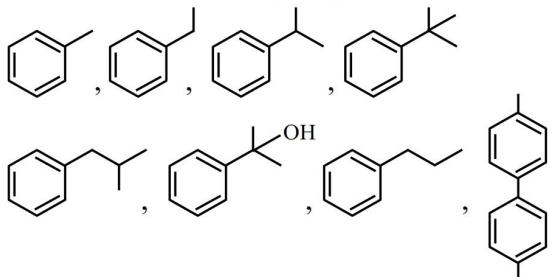
(C) $[\text{Co}(\text{NH}_3)_6]^{3+}$



(D) $[\text{Ni}(\text{CN})_4]^{2-}$



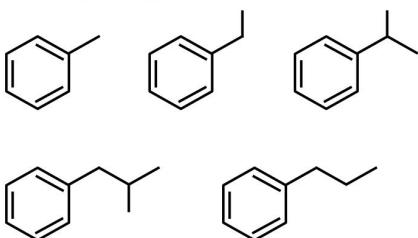
62. The total number of compounds from below when treated with hot KMnO_4 giving benzoic acid is :



- (1) 3
- (2) 4
- (3) 6
- (4) 5

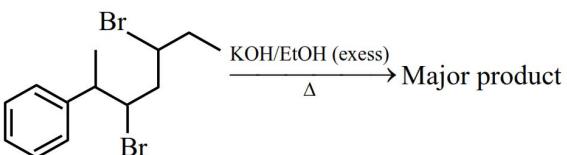
Ans. (4)

Sol. Compounds having at least 1 -H will react with KMnO_4 and give benzoic acid.



Total 5 compounds

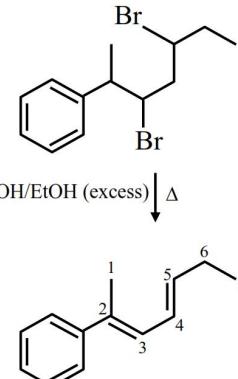
63. The major product of the following reaction is :



- (1) 6-Phenylhepta-2,4-diene
- (2) 2-Phenylhepta-2,5-diene
- (3) 6-Phenylhepta-3,5-diene
- (4) 2-Phenylhepta-2,4-diene

Ans. (4)

Sol.



2-Phenylhepta-2,4-diene

64. Given below are two statements :

Statement (I) : According to the Law of Octaves, the elements were arranged in the increasing order of their atomic number.

Statement (II) : Meyer observed a periodically repeated pattern upon plotting physical properties of certain elements against their respective atomic numbers.

In the light of the above statements, choose the **correct** answer from the options given below :

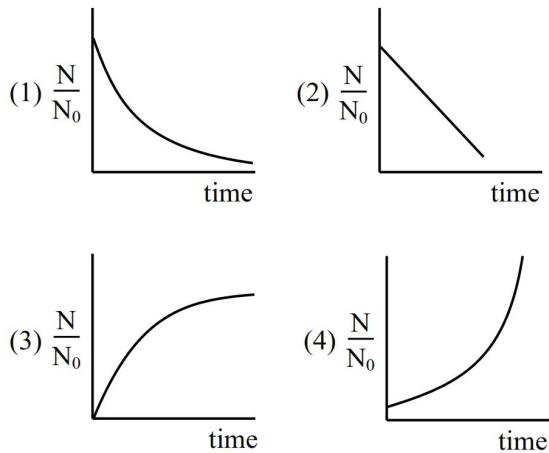
- (1) **Statement I** is false but **Statement II** is true
- (2) Both **Statement I** and **Statement II** are true
- (3) **Statement I** is true but **Statement II** is false
- (4) Both **Statement I** and **Statement II** are false

Ans. (4)

Sol. Law of octaves was arranged in the increasing order of their atomic weight.

Lothar Meyer plotted the physical properties such as atomic volume, melting point and boiling point against atomic weight.

65. For bacterial growth in a cell culture, growth law is very similar to the law of radioactive decay. Which of the following graphs is most suitable to represent bacterial colony growth?

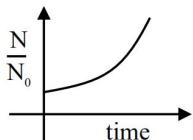


Ans. (4)

Sol. Because no. of bacteria initial = N_0 and No. of bacteria at any time t = N
Since bacterial growth is given as

$$N = N_0 e^{kt}$$

Where K = growth constant for bacterial growth



66. Which of the following is/are not correct with respect to energy of atomic orbitals of hydrogen atom?

(A) $1s < 2p < 3d < 4s$
 (B) $1s < 2s = 2p < 3s = 3p$
 (C) $1s < 2s < 2p < 3s < 3p$
 (D) $1s < 2s < 4s < 3d$

Choose the **correct** answer from the options given below :

(1) (B) and (D) only (2) (A) and (C) only
 (3) (C) and (D) only (4) (A) and (B) only

Ans. (3)

Sol. For single electron species energy only depends on 'n' (principal quantum number)
So energy of $2s = 2p$
and energy of $3d < 4s$

67. Assume a living cell with 0.9% (ω/ω) of glucose solution (aqueous). This cell is immersed in another solution having equal mole fraction of glucose and water.

(Consider the data upto first decimal place only)

The cell will :

(1) shrink since soluton is 0.5% (ω/ω)
 (2) shrink since solution is 0.45% (ω/ω) as a result of association of glucose molecules (due to hydrogen bonding)
 (3) swell up since solution is 1% (ω/ω)
 (4) Show no change in volume since solution is 0.9% (ω/ω)

Ans. (BONUS)

NTA (4)

Sol. Living cell = 0.9 gm in 100 gm of solution
 $\% \text{ w/w} = 0.9$
 Solution is have equal moles of glucose and water = 0.5
 Weight of solution = $0.5 \times 180 + 0.5 \times 18 = 99$ gm
 $\% \text{ w/w} \approx 90\%$
 Concentrated solution
 = Cell will shrink.

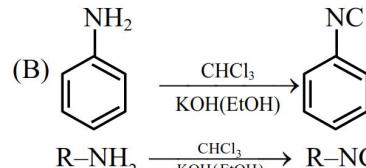
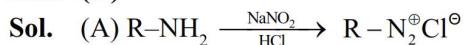
68. Identify correct statements :

(A) Primary amines do not give diazonium salts when treated with NaNO_2 in acidic condition.
 (B) Aliphatic and aromatic primary amines on heating wth CHCl_3 and ethanolic KOH form carbylamines.
 (C) Secondary and tertiary amines also give carbylamine test.
 (D) Benzenesulfonyl chloride is known as Hinsberg's reagent.
 (E) Tertiary amines reacts with benzenesulfonyl chloride very easily.

Choose the correct answer from the options given below :

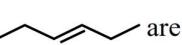
(1) (B) and (D) only (2) (A) and (B) only
 (3) (D) and (E) only (4) (B) and (C) only

Ans. (1)



(C) Only primary amine gives carbyl amine test
 (D) $\text{Ph}-\text{SO}_2\text{Cl} \longrightarrow$ Hinsberg reagent
 Benzene sulphonyl chloride
 (E) Tertiary amine do not react with $\text{Ph}-\text{SO}_2\text{Cl}$
 So correct options are (B) and (D) only

69. Given below are two statements :

Statement (I) :  and  are isomeric compounds.

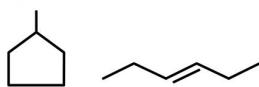
Statement (II) : NH₂ and  are functional group isomers.

In the light of the above statements, choose the **correct** answer from the options given below :

- (1) Both **Statement I** and **Statement II** are false
- (2) Both **Statement I** and **Statement II** are true
- (3) **Statement I** is true but **Statement II** is false
- (4) **Statement I** is false but **Statement II** is true

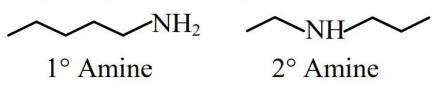
Ans. (2)

Sol. **Statement-I** \rightarrow True



Both are ring chain isomers

Statement-II \rightarrow True



1° Amine and 2° Amine are different functional groups, hence both are functional group isomers.

70. Identify the inorganic sulphides that are yellow in colour :

(A) (NH ₄) ₂ S	(B) PbS
(C) CuS	(D) As ₂ S ₃
(E) As ₂ S ₅	

Choose the **correct** answer from the options given below :

(A) (A) and (C) only	(2) (A), (D) and (E) only
(3) (A) and (B) only	(4) (D) and (E) only

Ans. (4)

NTA (2)

Sol. As₂S₃ and As₂S₅ are yellow colour sulphides, (NH₄)₂S is colourless, PbS is black, CuS is black in colour

SECTION-B

71. The spin only magnetic moment (μ) value (B.M.) of the compound with strongest oxidising power among Mn₂O₃, TiO and VO is _____ B.M. (Nearest integer).

Ans. (5)

Sol. Strongest oxidising power among the option is Mn₂O₃ because of E° value

$$E^\circ_{Mn^{+3}/Mn^{+2}} = +1.57V$$

Mn⁺³ \rightarrow d⁴ configuration

$$\mu = \sqrt{24} \text{ BM}$$

$$= 4.89 \text{ BM}$$

$$\Rightarrow 5$$

72. Consider the following data :

Heat of formation of CO₂(g) = -393.5 kJ mol⁻¹

Heat of formation of H₂O(l) = -286.0 kJ mol⁻¹

Heat of combustion of benzene = -3267.0 kJ mol⁻¹

The heat of formation of benzene is _____ kJ mol⁻¹. (Nearest integer)

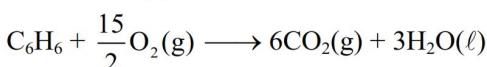
Ans. (48)

Sol. $\Delta H_f[\text{CO}_2(\text{g})] = -393.5 \text{ kJ / mole}$

$\Delta H_f[\text{H}_2\text{O}(\ell)] = -286.0 \text{ kJ / mole}$

$\Delta H_f[\text{C}_6\text{H}_6] = -3267.0 \text{ kJ / mole}$

$\Delta H_f[\text{C}_6\text{H}_6] = (?)$



$$\Delta H_R = \Delta H_C = \sum \Delta H_f(P) - \sum \Delta H_f(R)$$

$$-3267 = 6 \times (-393.5) + 3(-286) - \Delta H_f(\text{C}_6\text{H}_6)$$

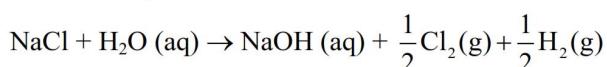
$$\Delta H_f(\text{C}_6\text{H}_6) = 48 \text{ kJ/mole}$$

73. Electrolysis of 600 mL aqueous solution of NaCl for 5 min changes the pH of the solution to 12.

The current in Amperes used for the given electrolysis is _____. (Nearest integer).

Ans. (2)

Sol. Electrolysis of NaCl is



Since during electrolysis pH changes to 12

$$\text{So } [\text{OH}^\ominus] = 10^{-2} \text{ and } [\text{H}^\oplus] = 10^{-12}$$

So by Faraday law

Gram amount of substance deposited =

Amount of electricity passed

$$10^{-2} \times \frac{600}{1000} \times 96500 = I \times t$$

$$\frac{10^{-2} \times 600}{1000} \times 96500 = I \times 5 \times 60$$

$$I = \frac{10^{-2} \times 600 \times 96500}{1000 \times 5 \times 60}$$

$$I = 1.93 \text{ ampere}$$

So, I = 2 ampere (nearest integer)

74. A group 15 element forms dπ-dπ bond with transition metals. It also forms hydride, which is a strongest base among the hydrides of other group members that form dπ-dπ bond. The atomic number of the element is _____.

Ans. (15)

Sol. Phosphorus belongs to 15th group and forms dπ-dπ bond with transition metal and PH₃ is strongest base among the other group members except NH₃.

75. Total number of molecules/species from following which will be paramagnetic is _____.
 $O_2, O_2^+, O_2^-, NO, NO_2, CO, K_2[NiCl_4],$
 $[Co(NH_3)_6]Cl_3, K_2[Ni(CN)_4]$

Ans. (6)

Sol. $O_2 \rightarrow 2$ unpaired electrons according to MOT
 $O_2^+ \rightarrow 1$ unpaired electrons according to MOT
 $O_2^- \rightarrow 1$ unpaired electrons according to MOT
 $NO \rightarrow$ odd electron species
 $NO_2 \rightarrow$ odd electron species
 $K_2[NiCl_4] \rightarrow Ni^{2+} \Rightarrow 3d^8$ weak Ligand, C.N. = 4
 \Rightarrow Tetrahedral, Paramagnetic with 2 unpaired electrons